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# Cross-shore distribution of the wave-induced circulation over a dissipative beach under storm wave conditions

- ${\bf Marc\ Pezerat}^1, {\bf Xavier\ Bertin}^1, {\bf K\acute{e}vin\ Martins}^2, {\bf Laura\ Lavaud}^1$
- $^{1}$ UMR 7266 LIENSs, CNRS/La Rochelle Université, 2 rue Olympe de Gouges, 17000 La Rochelle, France
- $_{\rm 5}$   $^2$  UMR 5805 EPOC, CNRS/Université de Bordeaux, Allée Geoffroy Saint-Hilaire, F-33615 Pessac, France

#### 6 Key Points:

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7	• Field experiment at a dissipative beach with $6 \text{ m } H_{m0}$ at breaking and undertow
8	reaching $0.2 \mathrm{m/s}$ as far as 4 km from the shoreline.
9	• Accurate reproduction of the cross-shore hydrodynamics using a phase-averaged 3I
10	circulation model.

- Strong sensitivity of the vertical mixing to breaking wave parameterization.
- Wave dissipation by breaking locally increases seaward-directed flows by over 100%
   compared to the surface Stokes drift velocity.

Corresponding author: Marc Pezerat, marc.pezerat@univ-lr.fr

#### 14 Abstract

This study explores the spatial distribution and the driving mechanisms of the wave-induced 15 cross-shore flow within the shoreface and surf zone of a dissipative beach. Unpublished re-16 sults from a field campaign carried out in early 2021 under storm wave conditions are 17 presented and compared with the predictions from a state-of-the-art phase-averaged three-18 dimensional circulation modelling system based on the vortex force formalism. Under storm 19 wave conditions, the cross-shore flow is dominated by a strong seaward-directed current in 20 the lower part of the water column. The largest current velocities of this return current 21 are located in the surf zone, where the dissipation by depth-induced breaking is most in-22 tense, but offshore-directed velocities up to  $0.2 \,\mathrm{m/s}$  are observed as far as 4 km from the 23 shoreline ( $\simeq 12$  m-depth). Numerical experiments further highlight the key control exerted 24 by non-conservative wave forces and wave-enhanced mixing on the cross-shore flow across a 25 transition zone, where depth-induced breaking, whitecapping and bottom friction all signif-26 icantly contribute to the wave energy dissipation. Under storm conditions, this transition 27 zone extended almost 6 km offshore and the cross-shore Lagrangian circulation shows a 28 strong seaward-directed jet in the lower part of the water column, whose intensity progres-29 sively decreases offshore. In contrast, the surf zone edge appears clearly delimited under 30 fair weather conditions and the seaward-directed current is weakened by a near bottom 31 shoreward-directed current associated with wave bottom streaming in the shoaling region, 32 such that the clockwise Lagrangian overturning circulation is constrained by an additional 33 anti-clockwise overturning cell at the surf zone edge. 34

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#### Plain Language Summary

As waves propagate toward the shore fluid parcels experience a net transport in the 36 direction of wave propagation. This onshore mass transport is compensated by a near bed 37 return flow, which dynamics remain poorly understood. This study combines measurements 38 from a field campaign carried out in early 2021 in front of a gentle sloping beach and 39 numerical modelling to explore the spatial distribution and the driving mechanisms of this 40 wave-induced cross-shore flow. Both observations and model results show that the largest 41 current velocities of this return current are located very close to the shoreline, where the 42 wave breaking is the most intense, but values up to  $0.2 \,\mathrm{m/s}$  are observed as far as  $4 \,\mathrm{km}$ 43 from the shoreline under storm conditions. Numerical experiments further highlight the 44 key control exerted by the wave forces and the wave-enhanced mixing, which induce very 45

- 46 contrasted circulation patterns under fair weather or storm conditions and strongly constrain
- 47 the vertical structure of the cross shore flow.

#### 48 1 Introduction

The nearshore circulation driven by breaking waves contributes to the cross-shelf transport of material, especially in the vicinity of the surf zone, such as the transport of nutrient (e.g. Morgan et al., 2018) or sediment, which can result in large morphological changes under storm conditions (e.g. Wright & Short, 1984; Coco et al., 2014; Castelle et al., 2015).

Considering a weak along-shore variability of the topography and a shore normal inci-53 dence of waves, the interplay between waves and currents most notably drives the so-called 54 undertow. Based on the depth-integrated continuity equation, the undertow commonly des-55 ignates the time- and depth-averaged Eulerian offshore flow compensating for the onshore 56 mass transport associated with the Stokes drift. The onshore-directed mass transport is 57 further enhanced within the surf zone due to contribution from surface wave rollers (e.g. 58 Svendsen, 1984a). The underlying dynamics were further investigated both theoretically 59 and experimentally, providing some insights onto the vertical structure of the (Eulerian) 60 cross-shore flow. Within the surf zone, several pioneering studies (e.g. Svendsen, 1984a; 61 Stive & Wind, 1986; Deigaard et al., 1991; Haines & Sallenger Jr, 1994; Garcez Faria et 62 al., 2000, among many others) proposed theoretical models, which all conceptually rely on 63 the local imbalance between the depth-uniform barotropic pressure gradient associated with 64 the wave setup and the depth-varying gradient of the wave radiation stresses. These models 65 adequately predict parabolic velocity profile, whose curvature is a function of local wave 66 quantities and the vertical eddy viscosity (e.g. Garcez Faria et al., 2000). 67

In contrast, the wave induced dynamics seaward of the surf zone received much less 68 attention, particularly under storm waves. Most notably, Lentz et al. (2008) combined long 69 term observations with a one-dimensional vertical model adapted from Xu and Bowen (1994) 70 to study the vertical structure of the cross-shore flow up to the inner-shelf. These authors 71 showed that the cross-shore velocity profiles seaward of the surf zone do not resemble the 72 parabolic profiles observed within the surf zone, but exhibit a maximum near the surface, 73 which is consistent with a balance between the Coriolis force associated with the offshore flow 74 and the Stokes-Coriolis force, also referred to as the Hasselmann wave stress (K. Hasselmann, 75 1970). As a result, the offshore flow tends to be equal in magnitude but opposite in direction 76

 $\pi$  to the onshore Stokes drift velocity all along the water column, which implies a nearly depth-

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uniform zero cross-shore Lagrangian flow seaward of the surf zone.

In recent years, wave-averaged three-dimensional (3D) circulation models have been 79 developed aiming to represent consistently the effect of short waves on the mean circulation 80 for a wide range of nearshore, coastal and open-ocean applications. Several theoretical ap-81 proaches were proposed on the form of the wave-modified primitive equations that would 82 be suitable for such models (e.g. see Bennis et al., 2011). The wave-averaged vortex force 83 formalism, which separates conservative and non-conservative wave forcing on the 3D quasi-84 Eulerian mean circulation, constitutes a theoretically-robust framework employed within 85 several of these modelling systems (e.g. Uchiyama et al., 2010; Kumar et al., 2012; Michaud 86 et al., 2012; Delpey et al., 2014; Zheng et al., 2017; Guérin et al., 2018). For nearshore appli-87 cations, non-conservative effects associated with wave energy dissipation processes through 88 depth-induced breaking, whitecapping and bottom friction are expected to play a crucial 89 role. While Smith (2006) consistently derived the contribution of these processes to the 90 depth-integrated momentum equations, no definite theory exists to express these terms for 91 the depth-resolving equations. In particular, it is assumed that the dissipation of wave en-92 ergy by breaking acts either like a surface stress on the mean flow or like a body force, in 93 which case one can thus impose an empirical vertical distribution such that the breaking 94 contribution applies at appropriate depths near the surface (e.g. Uchiyama et al., 2010). As 95 pointed out by Rascle (2007), the wave-enhanced vertical mixing associated with the pro-96 duction of turbulence by breaking waves mostly controls the vertical shear of the horizontal 97 current velocity so that the near-surface distribution of the momentum source sparsely mat-98 ters. In this regard, wave-averaged 3D circulation models are usually supplemented by a 99 two-equation turbulence closure model, which allows to approximate the wave-enhanced 100 turbulent kinetic energy (TKE) budget across the water column. There is a consensus in 101 the literature to model the TKE injection with a flux-type boundary condition at the water 102 surface assuming a power law for the decay of TKE (Umlauf & Burchard, 2003). Craig 103 and Banner (1994) proposed to express the surface flux of energy injected into the water 104 column in proportion to the surface wind friction velocity cubed. Following this approach, 105 it is assumed that the energy flux from the wind to the wave field very closely matches 106 that transferred from the wave field to the water column, which appears especially relevant 107 for the deep ocean where breaking processes (whitecapping) significantly impacts the at-108 mospheric drag coefficient. For nearshore applications however, observations support the 109

fact that the surface flux of TKE scales with the energy dissipated through depth-induced breaking (e.g. Feddersen & Trowbridge, 2005). It is also interesting to note that the decay of TKE near the surface is particularly sensitive to the surface mixing length, which remains an empirically parameterized quantity (e.g. see Moghimi et al., 2016).

Among the above mentioned studies, Uchivama et al. (2010), Kumar et al. (2012), 114 Michaud et al. (2012) and Zheng et al. (2017) essentially detailed the implementation of the 115 vortex force formalism within various modelling framework and further aimed to demon-116 strate the general applicability of this approach to study surf zone dynamics over commonly 117 used study cases, including applications at Duck, N.C., which serves as a reference bench-118 mark. In addition, Kumar et al. (2012) also reproduced the results from Lentz et al. (2008) 119 seaward of the surf zone using the same dataset. In a recent model-based study following 120 Uchiyama et al. (2010), Wang et al. (2020) further discussed the effect of the bottom wave 121 streaming, which is the stress along the direction of wave propagation that accompanies the 122 wave energy dissipation by bottom friction. Most notably, their results tended to show that 123 the Lagrangian overturning circulation within the surf zone could be substantially weakened 124 by an opposite overturning cell arising seaward of the surf zone and extending within it, 125 associated with the bottom wave streaming. Realistic applications of state-of-the-art, fully 126 coupled, wave-averaged 3D circulation models in the nearshore region remain very scarce 127 (Michaud et al., 2012; Delpey et al., 2014; Guérin et al., 2018), especially under storm 128 conditions, such that our comprehensive understanding of the wave-induced hydrodynamics 129 remains somehow limited and the predictive skills of these models uncertain. 130

This study aims to explore the cross-shore distribution and the driving mechanisms 131 of the wave-induced cross-shore circulation within the shoreface and the surf zone of a 132 dissipative beach. We present unpublished results from a field campaign carried out in 133 early 2021 in the central part of the French Atlantic coast under storm wave conditions, 134 complemented with predictions from the state-of-the-art 3D circulation model SCHISM 135 (Y. J. Zhang et al., 2016), fully coupled with the spectral wave model WWM (Roland et 136 al., 2012). The manuscript is organized as follows. The study area, the field campaign and 137 the processing of in-situ measurements are presented in Section 2. The parameterization 138 of the modelling system is detailed in Section 3 and its predictive skills are assessed in 139 Section 4 for the case study considered here. The section 5 discusses the contrasted wave-140 induced circulation patterns and associated driving mechanisms under high and moderate 141

- wave energy conditions based on further numerical experiments. Finally, concluding remarks
- <sup>143</sup> are provided in Section 6.

<sup>144</sup> 2 Study area and field campaign

#### 145 2.1 Study area

The study area is located along the South-Western coast of the Oléron Island in the 146 central part of the French Atlantic coast (see Fig. 1a), in front of Saint-Trojan Beach. This 147 beach corresponds to a 8 km-long sandspit bounded to the South by the Maumusson Inlet 148 and to the North by a rocky shore platform (Lavaud et al., 2020). In this region, tides 149 are semi-diurnal and range from 1.5 m to 5.5 m, which corresponds to a macrotidal regime. 150 Yearly mean wave conditions along the 30 m isobath are characterized by a significant wave 151 height of 1.6 m, a mean wave period of 5.9 s and a direction of  $285^{\circ}$  from the true North 152 (Dodet et al., 2019), but the offshore significant wave height can exceed 10 m with peak 153 periods over 20s (Bertin et al., 2015). This area is characterized by a very gently-sloping 154 shoreface (the isobath 20 m being found approximately 10 km offshore) and a non-barred dis-155 sipative beach composed of fine sandy sediments and exposed to an energetic wave climate. 156 Although this stretch of coast is relatively along-shore uniform, small amplitude inter-tidal 157 bars can develop after the persistence of fair weather conditions (see Bertin et al., 2008; 158 Guérin et al., 2018, for supplementary studies in this area). 159



Figure 1. a) Location of the study area in the Bay of Biscay, bathymetric map covering the computational domain (the open boundary is symbolised with the red dotted line) with isobaths reduced to the mean sea level displayed every 10 m (black dash-dotted lines), and position of the Chassiron meteorological station, AWAC, ADCP 600 kHz and inter-tidal area sensors. A cross-shore profile extending from the isobath 25 m to PT5 sensor is also displayed (brown dashed line).
b) Cross-shore profile from AWAC location to the first sensor deployed within the inter-tidal area.
c) Zoom on inter-tidal area sensors.

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#### 2.2 Field campaign and data processing

The field campaign was carried out between January and February 2021 in two steps. 161 First, two Acoustic Doppler Current Profilers (ADCP) were mounted on structures anchored 162 in the seabed, at approximately 12.5 m- and 7.5 m-depth locations below Mean Sea Level 163 (MSL) for a long-term deployment between the 19<sup>th</sup> of January and the 26<sup>th</sup> of February (see 164 Fig. 1). The most offshore instrument is a high resolution ADCP (1 MHz) integrating an 165 Acoustic Surface Tracker (AST) and is hereafter referred to as the AWAC, whereas the other 166 one is a medium-resolution ADCP (600 kHz). Both instruments alternated a "current cycle" 167 and a "wave cycle" each hour. During the current cycle, 10 min-averaged velocity profile 168 measurements were collected along the vertical axis, whereas during the wave cycle velocity 169 measurements within a fixed 2 m-high cell and pressure measurements were performed at 170

2 Hz during 20 minutes. Second, a set of sensors was deployed in the inter-tidal area (Fig. 171 1c) between the 29<sup>th</sup> and the 31<sup>st</sup> of January during spring tides so as to capture a highly 172 energetic event associated with the storm Justine. The offshore significant wave height at the 173 Biscay Buoy location (5°W, 45.23°N) reached 10 m, which corresponds to a return period 174 of the order of one year (Nicolae-Lerma et al., 2015). The swell associated with the storm 175 reached the study area during the night of the 30<sup>th</sup> from a westward direction, while local 176 winds reached 15 m/s at the storm peak. This set of sensors was deployed along a cross-shore 177 profile and included one 2 MHz ADCP (with a similar data collection scheme than for the 178 two offshore ADCPs), three pressure transducers with a 2 Hz sampling frequency (PT) and 179 one Acoustic Doppler Velocimeter deployed 20 cm above the seabed, with a 16 Hz sampling 180 frequency (ADV). The PTs and ADV all performed continuous measurements. 181

For each sensor, sea-bottom pressure timeseries were split into 20 min-long bursts 182 (consistent with ADCPs "wave cycle"), corrected for sea level atmospheric pressure using 183 data collected at the nearby meteorological station of Chassiron (Fig. 1a), detrended and 184 converted into a sea-surface elevation signal assuming a hydrostatic pressure. For the sen-185 sors deployed in the inter-tidal area, measurements below a burst-averaged water depth of 186 0.5 m were discarded due to the presence of substantial infra-gravity waves, which caused 187 the sensors to be intermittently dry. Then, pressure attenuation with depth due to non-188 hydrostatic effects was corrected using the Transfer Function Method based on the linear 189 wave theory (TFM, e.g. Bishop & Donelan, 1987). This method requires an upper cutoff 190 frequency to remove high frequency noise that is amplified by the TFM correction, and to 191 prevent the over-amplification of high-frequency energy levels due to non-linear interactions 192 in intermediate and shallow-water depths (Mouragues et al., 2019). The cutoff frequency 193 was set to 0.2 Hz for the two offshore sensors and 0.4 Hz for the sensors in the inter-tidal 194 area. Finally, the sea surface elevation density spectra E(f) were computed by means of a 195 Fast Fourier Transform on 10 Hanning-windowed segments with a 50% overlap, which al-196 lows a good compromise between statistical stability (20 degrees of freedom) and frequency 197 resolution  $(8.3 \,\mathrm{mHz})$ . The processing of pressure measurements was further verified at the 198 AWAC location by comparing the sea-surface elevation spectra with those obtained from 199 the AST measurements. These measurements were not used directly due to spurious sig-200 nals during the most energetic events, whose are probably explained by the presence of air 201 bubbles in the water column induced by the breaking of storm waves (not shown). Wave 202 bulk parameters (significant wave height,  $H_{m0}$ , mean and continuous peak periods,  $T_{m02}$ 203

and  $T_{pc}$ ) were computed using the  $p^{\text{th}}$  moments of the spectra:

$$m_p = \int_{f_{min}}^{f_c} f^p E(f) df \tag{1}$$

206 such that:

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$$H_{m0} = 4\sqrt{m_0} 
 T_{m02} = \sqrt{\frac{m_0}{m_2}} 
 T_{pc} = \frac{m_{-2}m_1}{m_0^2}$$
(2)

For each sensor, an adaptive  $f_{min}$  value, defined as half the continuous peak frequency computed at the AWAC location, was used in order to separate the gravity from the infragravity bands (e.g. Hamm & Peronnard, 1997; Bertin et al., 2020).

For the two offshore ADCPs, 10 min-averaged vertical profiles of current velocities were 211 acquired along bins spanned respectively every 1 m (AWAC) and 0.5 m (ADCP 600 kHz). 212 The measurements above a distance equal to the water depth minus half the significant wave 213 height were discarded due to contamination by surface reflections from the sidelobes of the 214 ADCP acoustic pulses (Appell et al., 1991). Current velocity profile measurements from the 215 ADCP 2MHz deployed in the inter-tidal area were discarded because of spurious bin-to-bin 216 velocity differences. Finally, continuous velocity measurements from the ADV, were split 217 into 30 min-long bursts and filtered from spikes using the phase-space thresholding method 218 of Goring and Nikora (2002). 219

The inter-tidal topography was surveyed at low tide during the deployment (29/01/2021)220 and the recovery (31/01/2021) of the instruments with PPK GNSS over an area centered on 221 the instrumented transect and extending 1 km along-shore. The comparison between both 222 datasets showed very limited morphological changes (with a root mean square difference of 223 0.10 m along the instrumented profile), a behaviour already reported by Guérin et al. (2018) 224 under similar storm wave conditions. The subtidal bathymetry was surveyed at the location 225 of the instrumented profile up to a water depth of 11 m below MSL four weeks after the 226 deployment in the inter-tidal area by means of a Norbit multi-beam echo-sounder. This 227 bathymetric dataset was merged with an extensive single-beam echo-sounder survey carried 228 out in April 2013. Both datasets in the region where they overlap show a smooth transition 229 in the subtidal zone with changes of the order of 0.4 m. 230

#### 3 Modelling system

The modelling system used in this study couples the 3D circulation model SCHISM 232 (Y. J. Zhang et al., 2016) and the third generation spectral wave model WWM (Roland et 233 al., 2012). This modelling system offers the flexibility to cover large geographic areas with 234 unstructured grid and very robust numerical schemes for both models. The 3D wave-induced 235 circulation is modelled through the vortex force formalism, such as presented by Bennis et 236 al. (2011). Its detailed implementation in SCHISM can be found in Guérin et al. (2018) and 237 is recalled in Appendix A. In the following, only the parameterization of the relevant part 238 of the model and further improvements since Guérin et al. (2018) are described. 239

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#### 3.1 Parameterization of WWM

#### 3.1.1 Depth-induced breaking parameterization

The wave energy dissipation rate by depth-induced breaking is computed according to the model of Battjes and Janssen (1978) with an adaptive breaking coefficient (*B*) as proposed by Pezerat et al. (2021). The local mean (phase-averaged) rate of energy dissipation per unit area  $D_{db}$  in (W/m<sup>2</sup>) reads:

$$D_{db} = \frac{B}{4} \rho g f_{mean} Q_b H_m^2 \tag{3}$$

where  $B = 40 \tan \beta$ , with  $\tan \beta$  the local bottom slope;  $f_{mean}$  is a mean frequency, usually computed as the ratio  $m_1/m_0$  (see Eq. 1);  $Q_b$  is the local fraction of breaking (and broken) waves and  $H_m$  is the local maximum possible wave height estimated by means of a parameterized Miche-type breaking criterion. Under the shallow water assumption,  $H_m$ reads:

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$$H_m = \gamma h \tag{4}$$

where  $\gamma$  is the breaking index, an adjustable coefficient, usually kept constant at 0.73 fol-253 lowing the calibration performed by Battjes and Stive (1985). However, as pointed out 254 by Pezerat et al. (2021), the introduction of the adaptive breaking coefficient requires a 255 newly calibrated breaking index. Based on sensitivity tests performed with the model on 256  $H_{m0}$  results considering the entire dataset (not shown), a constant value of  $\gamma = 0.60$  was 257 considered for this study. It is worth noting that this value might show some site- or wave 258 conditions-specificity, but it is not the purpose of this study to propose an extensive calibra-259 tion of the breaking index. Finally, following the approach of Eldeberky and Battjes (1996), 260

the corresponding source term in WWM is computed by distributing  $D_{db}$  over frequencies and directions in proportion to the spectral action density:

$$S_{db} = -\frac{D_{db}}{E_{tot}} N \text{ where } E_{tot} = \rho g \int_{\sigma} \int_{\theta} E d\sigma' d\theta'$$
(5)

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#### 3.1.2 Other source terms

The wind input  $(S_{in})$  and dissipation by whitecapping  $(S_{ds})$  are formulated according 265 to the parameterization of Ardhuin et al. (2010). Non-linear quadruplet interactions  $(S_{nl,4})$ 266 are taken into account following the approach of S. Hasselmann et al. (1985), whereas the 267 non-linear triad interactions  $(S_{nl,3})$  are parameterized following the approach of Eldeberky 268 (1997). Finally, the formulation of the energy dissipation by bottom friction  $(S_{bf})$  is adapted 269 from Tolman (1994). This formulation is based on the model of Madsen et al. (1988) 270 with a parameterization of the roughness issued from Grant and Madsen (1982), and was 271 subsequently adapted by Ardhuin et al. (2003) based on the SHOWEX experiment. 272

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#### 3.2 Parameterization of SCHISM

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#### 3.2.1 Non-conservative wave forces

The non-conservative wave forcing due to wave breaking  $[F_{br,x}, F_{br,y}]$  includes the effect of whitecapping and depth-induced breaking further modified due to the action of wave rollers (cf. Appendix A for the description of the roller model):

$$[\hat{F}_{br,x},\hat{F}_{br,y}] = \frac{\delta_{z,\bar{\eta}}}{\rho} \left( -\int_{\sigma} \int_{\theta} k \left( (1-\alpha_R)S_{db} + S_{ds} \right) \left[ \cos\theta', \sin\theta' \right] d\sigma' d\theta' + \frac{D_R}{\sigma_p} k_p \left[ \cos\theta_m, \sin\theta_m \right] \right)$$
(6)

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where the vertical distribution function is given by a delta function  $\delta_{z,\bar{\eta}}$ , such that the breaking-induced momentum is injected within the first cell below the free surface (Bennis et al., 2011). The roller model shows bearly any effect at both offshore locations, while the current intensity slightly increases with  $\alpha_R$  at the ADV location (not shown). The model best-fit results were obtained with  $\alpha_R = 0.5$ .

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The bottom streaming corresponds to the stress along the direction of wave propagation that accompanies the dissipation of wave energy by bottom friction within the wave boundary layer (Longuet-Higgins, 1953). The corresponding body force  $[F_{ws,x}, F_{ws,y}]$  is formulated by means of an upward decaying vertical distribution of the wave energy dissipation  $_{288}$  by bottom friction (Uchiyama et al., 2010):

$$[\hat{F}_{ws,x}, \hat{F}_{ws,y}] = -\frac{f^{ws}(z)}{\rho} \int_{\sigma} \int_{\theta} kS_{bf}[\cos\theta', \sin\theta'] d\sigma' d\theta'$$
(7)

where  $f^{ws}$  is a vertical distribution function given by:

$$f^{ws}(z) = \frac{1 - \tanh(k_{wd}(d+z))^2}{\int_{-d}^{\bar{\eta}} 1 - \tanh(k_{wd}(d+z))^2 dz}$$
(8)

where  $1/k_{wd} = a_{wd}\delta_{wbl}$  is a decay length proportional to the wave boundary layer thickness 292  $(\delta_{wbl})$ . Within SCHISM,  $\delta_{wbl}$  is derived from the wave boundary layer model of Madsen 293 (1995) that is used to compute the apparent roughness length for the parameterization of 294 the bottom friction within the circulation model (cf. section 3.2.3). The proportionality 295 coefficient  $a_{wd}$  is taken equal to unity, such that the decay length matches the theoretical 296 wave boundary layer thickness for monochromatic waves although laboratory measurements 297 of the bottom boundary layer under random waves suggest a significant increase in the 298 thickness, i.e.  $a_{wd} > 1$  (Klopman, 1994). 299

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#### 3.2.2 Wave-enhanced turbulence at the surface

The circulation model is supplemented by a  $K - \omega$  turbulence closure model retrieved from the Generic Length Scale (GLS) two-equation turbulence closure model within the framework of the General Ocean Turbulence Model (GOTM, Burchard et al., 1999; Umlauf et al., 2005). At the water surface, the turbulence closure model accounts for a TKE injection by breaking waves (K in m<sup>2</sup>/s<sup>2</sup>) through a flux-type boundary condition assuming a power law for the vertical decay of K (Umlauf & Burchard, 2003), which reads:

$$\frac{\nu}{\sigma_K} \frac{\partial K}{\partial z} = F_K \left( \frac{z_0^s - z'}{z_0^s} \right)^{\frac{3}{2}\alpha} \text{ at } z = \bar{\eta}$$
(9)

where  $F_K$  (in m<sup>3</sup>/s<sup>3</sup>) is the surface flux of energy injected into the water column,  $\nu$  is the 308 vertical eddy viscosity,  $\sigma_K$  is the turbulent Schmidt number for K,  $\alpha$  is the spatial decay 309 rate of TKE in the wave enhanced layer,  $z_0^s$  is the surface mixing length and z' is the distance 310 below the surface at which the flux is imposed. For numerical reason, z' is prescribed as 311 half the height of the top cell, such that the boundary condition for K requires a refined 312 discretization of the vertical grid near the surface. The surface mixing length  $(z_0^s)$  controls 313 the depth of penetration for the injected TKE. There are strong uncertainties over this 314 quantity, which has been either parameterized as a constant (e.g.  $z_0^s = 0.2 \,\mathrm{m}$ , Feddersen 315 & Trowbridge, 2005) or as a function of the significant wave height:  $z_0^s = \alpha_w H_{m0}$ , with 316  $\alpha_w = \mathcal{O}(1)$  (see Moghimi et al., 2016, for a short review). Following the approach of 317

Feddersen and Trowbridge (2005), the surface flux of TKE injected at the surface scales with the energy dissipated through wave-related processes at the surface:

$$F_K = \frac{c_{db}}{\rho} \left( -(1 - \alpha_R) \int_{\sigma} \int_{\theta} \sigma' S_{db} d\sigma' d\theta' + D_R \right) - \frac{c_{ds}}{\rho} \int_{\sigma} \int_{\theta} \sigma' S_{ds} d\sigma' d\theta'$$
(10)

where the coefficients  $c_{db}$  and  $c_{ds}$  control the amount of energy injected to the water column. The range of value 0.01 to 0.25 has been proposed in the literature for  $c_{db}$  (e.g. Feddersen & Trowbridge, 2005; Huang et al., 2009; Feddersen, 2012a, 2012b), while Paskyabi et al. (2012) suggest  $c_{ds} \simeq 1$ . The model best-fit results were obtained with  $z_0^s = \alpha_w H_{m0}$ ,  $\alpha_w = 1$ ;  $c_{db} = 0.15$  and  $c_{ds} = 1$ .

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#### 3.2.3 Bottom boundary condition

The bottom boundary condition imposes a balance between the internal Reynolds stress and the bottom frictional stress  $[\tau_{b,x}, \tau_{b,y}]$ :

$$\nu \frac{\partial [\hat{u}, \hat{v}]}{\partial z} = \frac{[\tau_{b,x}, \tau_{b,y}]}{\rho} \text{ at } z = -d$$
(11)

The law of the wall is then assumed, leading to a logarithmic profile for the velocity within a constant stress layer that presumably contains the bottom cell while the bottom stress is formulated with a quadratic bottom drag parameterization. The bottom stress finally reads (e.g. Blumberg & Mellor, 1987):

$$[\tau_{b,x}, \tau_{b,y}] = \rho C_d \sqrt{\hat{u}_b^2 + \hat{v}_b^2} [\hat{u}_b, \hat{v}_b] \text{ with } C_d = \left(\frac{\kappa}{\ln\left(\frac{\delta_b}{z_0}\right)}\right)^2 \tag{12}$$

where  $C_d$  is the friction factor,  $[\hat{u}_b, \hat{v}_b]$  is the velocity at the top of the bottom computational 335 cell,  $\kappa$  is the von Kármán's constant,  $\delta_b$  is the thickness of the bottom cell (in m) and  $z_0$  is 336 the bottom roughness length (in m). In the presence of waves, the wave-current interaction 337 theory by Madsen (1995) as modified by Mathisen and Madsen (1999) is applied to compute 338 an apparent roughness length  $z_0^a$ , which further replaces  $z_0$  in the expression of  $C_d$ , and 339 thus allows to account for the enhanced roughness experienced by the current in presence of 340 waves. This approach takes as input a (physical) bottom roughness length  $(z_0)$  to provide 341 an expression of the wave boundary layer thickness and  $z_0^a$  following a numerical procedure 342 described in H. Zhang et al. (2004). In this study,  $z_0$  varies spatially between 0.1 mm and 343 5 mm to account for the seabed granulometric variability based on the sea-bottom nature 344 map provided by the Hydrographic and Oceanographic French Office. 345

346

#### 3.3 Model implementation

The coupling between SCHISM and WWM is made at the source code level. Both 347 models share the same unstructured grid and domain decomposition. The horizontal spatial 348 resolution ranges from 2 km at the offshore boundary down to 20 m in the surf zone. The 349 vertical grid for the circulation model is discretized using 25 S-levels stretched near the 350 surface and the bottom. The time step for the circulation model is set to 10s whereas 351 WWM is running in implicit mode (Booij et al., 1999; Abdolali et al., 2020). This allows to 352 relax the constraint for the time step of the wave module, which was set to 300 s. Finally, the 353 spectral space in WWM was discretized in 36 directions covering the entire trigonometric 354 circle and 24 frequencies ranging from 0.03 to 0.4 Hz. 355

At the domain offshore boundaries, the tidal forcing was computed considering the 16 356 main constituents linearly interpolated from the regional tidal model of Bertin et al. (2012), 357 whereas WWM was forced with timeseries of energy spectra obtained from a North Atlantic 358 application of the spectral wave model WaveWatch III (WW3, Tolman, 1991). For both 359 SCHISM and WWM, the atmospheric forcing consisted of MSL pressure and wind speed at 360 10 m issued from the meteorological operational model ARPEGE (e.g. Déqué et al., 1994), 361 interpolated onto a  $0.1^{\circ}$  regular grid. WW3 was forced with wind fields at 10 m originating 362 from the Climate Forecast System Reanalysis (CFSR, Saha et al., 2011) extracted from 363 a  $0.2^{\circ}$  regular grid covering the entire North Atlantic basin. ARPEGE was preferred to 364 CFSR for our local application of the modelling system considering its slightly improved 365 predictive skills as compared to measurements of wind speed and direction at the nearby 366 meteorological station of Chassiron (Fig. 1). 367

#### 4 Observations and predictive skills of the model

A comparison between measurements and model best-fit results (run Rref) is presented. The overall model performance for each quantity is assessed with the normalized bias (NB) and the normalized root mean square error (NRMSE):

$$NB(X) = \begin{cases} \frac{\overline{\hat{X} - X}}{(\max X - \min X)} \times 100 \text{ if } \overline{X} \simeq 0\\ \frac{\overline{\hat{X} - X}}{\overline{X}} \times 100 \end{cases}$$
(13)

373

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$$\operatorname{NRMSE}(X) = \begin{cases} \frac{\sqrt{(\hat{X} - X)^2}}{(\max X - \min X)} \times 100 \text{ if } \overline{X} \simeq 0\\ \sqrt{\frac{(\hat{X} - X)^2}{\overline{X^2}}} \times 100 \end{cases}$$
(14)

where X and  $\hat{X}$  respectively correspond to the measured and modelled quantity and the overbar denotes the average over the timeseries.

377

#### 4.1 Water levels and short waves

Phase-averaged surface elevation variations are very well reproduced by the model at 378 the AWAC and ADCP 600 kHz locations (Fig. 2a-b), with a NRMSE lower than 6% obtained 379 at both locations. The negative bias observed at the AWAC location (NB = -4.1%) could 380 be attributed to pressure sensor drift, as it increases in time while such bias is not observed 381 at the nearby ADCP 600 kHz location. Model results on short waves are compared to 382 observations by means of bulk parameters computed with moments integrated over the same 383 frequency range as the data. These are very well reproduced by the model at both locations 384 (Fig. 2c-h) with a NRMSE on both  $H_{m0}$  and  $T_{m02}$  below 7%, only the continuous peak 385 period is slightly underestimated at the storm peak, resulting in a negative NB of -7.3% at 386 the ADCP 600 kHz location. This problem might be explained by the fact that spectral wave 387 models allow to represent energy transfers towards higher harmonics by sum self interactions 388 with the LTA formulation of (Eldeberky, 1997) but not by difference interactions. Thus, 389 the model cannot represent transfers from the gravity band towards the IG band and the 390 subsequent transfers back to the gravity band by the generation of IG wave higher harmonics 391 (e.g. Bertin et al., 2020), nor direct transfers towards low frequencies in the gravity band 392 (e.g. De Bakker et al., 2015). Both field measurements at the ADCP 600 kHz location and 393 model results show that  $H_{m0}$  is tidally modulated when exceeding approximately 2 m at the 394 AWAC location (Fig. 2d). Such modulation also occurs at the storm peak at the AWAC 395 location ( $H_{m0} \simeq 6$  m, Fig. 2c). This clearly suggests that depth-induced breaking starts 396 being substantial as far as 4 km away from the shoreline ( $\simeq 12.5 \,\mathrm{m}$ -depth) under energetic 397 conditions. In addition  $T_{m02}$  period is also tidally modulated, highlighting the significant 398 contribution of the non-linear triad interactions, whose intensity varies with the water-depth. 399 As the water-depth decreases, more energy is transferred towards the higher harmonics by 400 non-linear triad interactions, such that  $T_{m02}$  decreases. Within the inter-tidal area most 401 of the differences between model results and measurements are observed for water-depths 402 below 1 m (see Fig. 3). Water levels and significant wave heights are well reproduced by 403 the model with a NRMSE computed over all sensors that respectively reaches 10.4% and 404 10.8%. The  $T_{m02}$  period is not shown because a significant amount of energy is transferred 405 towards the IG band, which can partly go back to the gravity band through the generation 406

- of IG wave higher harmonics (Bertin et al., 2020), resulting in an increase of  $T_{m02}$ , a process
- that cannot be reproduced by the phase-averaged model.



Figure 2. Measured and simulated phase-averaged free surface elevation  $(\bar{\eta})$ , significant wave height  $(H_{m0})$ , mean period  $(T_{m02})$  and continuous peak period  $(T_{pc})$  timeseries at the AWAC (left panels) and ADCP 600 kHz (right panels) locations using the configuration of reference (Rref).



Figure 3. Measured and simulated water depth (a) and  $H_{m0}$  (b) scatter plot at the inner surfzone sensors locations using the configuration of reference (Rref).

409

#### 4.2 Cross-shore circulation

The model results for Rref on the cross-shore velocity component show a fairly good 410 agreement with measurements from the AWAC and the ADCP 600 kHz as shown Fig. 4 411 below the lowest sea surface tidal level. Overall, the NRMSE varies between 13.9% and 20%, 412 while the NB fluctuates between -2.9% and 5.6%. Note, however, that measurements from 413 the ADCP 600 kHz are more scattered under energetic wave conditions. First, this might 414 be partly due to measurement artefacts associated with the generation of bubbles in the 415 water column by depth-induced breaking, which is particularly active at this location (cf. 416 section 4.1). Second, as vertical current profile measurements are 10 min-averaged, there 417 may be an aliasing of the signal associated with currents induced by IG waves, whose period 418 can exceed 300s at this beach under storm conditions (Bertin et al., 2020). As averaging 419 currents over a longer period within a thicker cell results in a more accurate measurement 420

of the current velocity, we arbitrarily discarded current profile velocity measurement that 421 departed by more than  $0.15 \,\mathrm{m/s}$  from the 20 min-averaged velocity measurement performed 422 during the wave cycle within the fixed 2 m-high cell (see the red triangles in Fig. 4). Both 423 model results and measurements clearly show that the cross-shore velocity is mostly offshore-424 directed under energetic wave conditions reaching almost -0.5 m/s at the AWAC location 425 around the 31/01/2021. The model results for a run performed without waves (Rnowave), 426 which only accounts for the tides and the atmospheric forcing, show a strong positive bias 427 at both locations (e.g. the NB reaches 27.3% at the ADCP 600 kHz location), so that the 428 comparison between Rref and Rnowave highlights the significant contribution of the wave-429 induced current to the cross-shore flow. Based on this comparison, the contribution of the 430 wave-induced current at the peak of the storm reaches as much as  $0.25 \,\mathrm{m/s}$ . 431



**Figure 4.** Measured and simulated cross-shore velocity component timeseries at the AWAC (left panel) and ADCP 600 kHz (right panel) locations displayed for each vertical bin below the sea surface lowest level. Model results are presented for the run of reference (Rref) and for a run performed without waves (Rnowave). Red triangles tag the discarded measurements. The vertical position of each bin (denoted b) is measured from the bottom and hab stands for height above the sea-bed. The time range of the storm event is delimited by the grey background.

At the ADV location, burst-averaged cross-shore velocity measurements are quite scat-432 tered, especially during the second and third tidal cycle with fluctuations reaching  $0.2 \,\mathrm{m/s}$ . 433 The 30-min averaged current velocities suggest the presence of Very Low Frequency oscilla-434 tions (VLF, frequencies below 4 mHz), while IG waves contribution was presumably filtered. 435 The analysis of the whole dataset revealed that waves were mostly normally incident during 436 the storm event, which is quite common during energetic event at this site (Bertin et al., 437 2008). As a consequence, mean longshore currents remained weak during the field campaign 438 (ranging from -0.10 to 0.15 m/s) and were alternatively northward and southward-directed 439 within a very wide surf zone (not shown). Shear instabilities of mean longshore currents, 440 which require the presence of a strong shear (e.g., associated with highly-oblique large 441 waves breaking over a bar, see Oltman-Shay et al., 1989; Noyes et al., 2004) cannot there-442 fore explain such VLF motions. Instead, it could be attributed to the breaking of energetic 443 wave groups that has been identified as a mechanism for the generation of surf zone eddies 444 through the generation of vorticity at the scale of individual waves or wave groups (Long 445 & Ozkan-Haller, 2009; Feddersen, 2014), which is then transferred to VLF frequencies and 446 larger spatial scales through non-linear inverse energy cascades (Feddersen, 2014; Elgar & 447 Raubenheimer, 2020). 448

These complex dynamical features cannot be reproduced by the present phase-averaged 449 modelling approach, which undermines the comparison with the field observations (the 450 NRMSE on the cross-shore velocity component reaches 24.9%). Both model results and 451 observations qualitatively show that the cross-shore velocity component is dominated by a 452 wave-induced seaward-oriented current, whose intensity increases with the significant wave 453 height (Fig. 5b-c). As more energy is dissipated by depth-induced breaking when the sig-454 nificant wave height increases, it further suggests that non-conservative breaking wave force 455 strengthens locally this seaward-oriented current. 456





Figure 5. Measured and simulated water depth,  $H_{m0}$  and cross-shore velocity component timeseries at ADV location.

#### $_{457}$ 5 Discussion

The results clearly show that the wave-induced circulation plays a crucial role on the 458 cross-shore flow. Circulation patterns show a strong seaward-directed current in the lower 459 part of the water column as far as 4 km from the shoreline, which cannot be reproduced by 460 solely accounting for the wind and the tidal forcing. This unsteady cross-shore circulation is 461 quite well reproduced by the model, which shows excellent predictive skills for short waves 462 with errors on bulk parameters ranging from 4 to 9%. Switching off the wind does not 463 significantly impact the results on short waves because the local wave growth remains weak 464 (not shown). A new configuration of the model was thus setup with wind and tidal forcing 465 switched off in order to investigate the driving mechanisms of the wave-induced circulation 466 while bypassing the unsteadiness associated with tides and wind. This configuration was 467 run for two distinct 24 h-periods associated with storm waves ( $H_{m0} = 5.3 \text{ m} - 30/01/2021$ ) 468 and moderate wave energy conditions  $(H_{m0} = 2.0 \text{ m} - 04/02/2021)$ . 469

#### 470 **5.1 Wa**

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#### 5.1 Wave energy dissipation patterns

<sup>471</sup> Considering the significant contribution of the wave energy dissipation processes either <sup>472</sup> on the TKE injection or through the non-conservative wave forces, the energy dissipation <sup>473</sup> rates associated with depth-induced breaking  $(D_{db})$ , whitecapping  $(D_{ds})$  and bottom friction <sup>474</sup>  $(D_{bf})$  are first examined following the approach of Pezerat et al. (2021), based on the <sup>475</sup> empirical ratio R reading:

$$R = \frac{D_{db}}{(D_{ds} + D_{bf} + D_{db})} \text{ with } D_x = \int_{\sigma} \int_{\theta} \sigma' S_x d\sigma' d\theta'$$
(15)

where the subscript x represents either of the "db", "ds" or "bf" subscripts. As shown 477 in Fig. 6 along a cross-shore profile (see Fig. 1), one can distinguish three typical areas. 478 Offshore (zone I, R < 0.1), wave energy dissipation is mostly associated with bottom friction. 479 Closer to shore, a transition zone appears (zone II, 0.1 < R < 0.9), within which bottom 480 friction, whitecapping and depth-induced breaking together significantly contribute to the 481 incident wave energy dissipation, before depth-induced breaking becomes dominant (zone 482 III, R > 0.9). Most notably, the transition zone is much wider under high wave energy 483 conditions (approximately 6 km-long spaning from approximately 15 m- to 5 m-depth) than 484 under moderate wave energy conditions (less than 1 km-long with water depth comprised 485 between 5 m and 7 m). The edge of the third zone is approximately located at the same 486 distance from the shoreline in both situations ( $\simeq 5$  m-depth). Interestingly, the wave energy 487 dissipation rates associated with whitecapping and bottom friction are of the same order 488 within the zones I and II under high wave energy conditions, and even dominate the depth-489 induced breaking contribution over approximately 5 km up to a water-depth of the order 490 of  $15 \,\mathrm{m}$  (Fig. 6a). Although it is commonly understood that the surf zone is widening 491 under storm waves, it appears more appropriate to introduce this conceptual transition 492 zone, while the third zone more likely corresponds to the inner surf zone. It is worth noting 493 that the development of this wide transition zone is also presumably related to the gentle 494 and smoothly increasing bottom slope that characterizes the study area, while the transition 495 to a regime dominated by depth-induced breaking is much more abrupt over barred beach or 496 fringing environments. It would be thus interesting to perform similar analysis in contrasted 497 environments, with a diversity of beach profiles and bottom substrate. 498

The roller model shows a weak effect on the location where energy is dissipated. This could be presumably attributed to the gentle bottom slope characterizing the study area,

- while previous studies highlighted the significant roller effect over a barred and steeper beach
- <sup>502</sup> (e.g. Reniers et al., 2004; Uchiyama et al., 2010; Kumar et al., 2012; Zheng et al., 2017).



Figure 6. Wave energy dissipation rates profiles associated with bottom friction  $(D_{bf})$ , whitecapping  $(D_{ds})$ , depth-induced breaking  $(D_{db})$  and roller energy dissipation rates  $((1-\alpha_R)D_{db}+D_R)$ under high (a) or moderate (b) wave energy conditions.

503

#### 5.2 Sensitivity to vertical mixing

The results presented above show a substantial wave energy dissipation associated with whitecapping and depth-induced breaking as far as 6 km from the shoreline under energetic conditions, which further suggest that a substantial amount of TKE could be injected at the surface. Three principal parameters control the injection of TKE at the surface ( $c_{db}$  and  $c_{ds}$ ) and its vertical decay ( $z_0^s$ ). If we consider the default value taken for  $c_{db}$  and  $c_{ds}$ , we note that for equivalent energy dissipated through whitecapping and depth-induced breaking (i.e.  $D_{ds} \sim D_{db}$ ), more weight is given to the whitecapping contribution. Previous studies have

highlighted the effect of breaking-wave-generated turbulence on the mean circulation within 511 the surf zone, which results in a reduction of the vertical shear of the horizontal current 512 (e.g. Feddersen & Trowbridge, 2005; Kumar et al., 2012). In intermediate water depths, 513 Paskyabi et al. (2012) showed that surface currents associated with Ekman transport are 514 better reproduced when accounting for whitecapping contribution to the wave-enhanced 515 mixing, while Lentz et al. (2008) used a crude parameterization based on the wind stress 516 for the vertical eddy viscosity for their study over the inner continental shelf. Overall, the 517 contribution of the wave-enhanced turbulence to the mean circulation under the combined 518 effects of depth-induced breaking and whitecapping has thus never been evaluated across 519 the shoreface (note that Kumar et al., 2012, gathered both contributions to compute the 520 surface flux of TKE and used  $c_{db} = c_{ds}$ ). In addition, a sensitivity analysis of the vertical 521 shear of the mean cross-shore current to the parameterization of the surface mixing length 522  $z_0^s$  was performed to supplement the study of Moghimi et al. (2016), who highlighted the 523 sensitivity of turbulence closure models to  $z_0^s$  because of the power law for the decay of the 524 TKE. Three additional runs were thus retained (see Table 1) to assess the sensitivity of the 525 vertical mixing to the parameterization of the TKE injection and how it further impacts 526 the cross-shore circulation. The results are compared along vertical profiles of TKE (K), 527 vertical eddy viscosity ( $\nu$ ) and cross-shore quasi-Eulerian velocity component ( $\hat{u}$ ) distributed 528 along the aforementioned cross-shore profile (see Fig. 7 and Table 2). 529

Table 1. Turbulence settings for the runs Rref, Rturb1, Rturb2 and Rturb3. The mixing length increases with  $\alpha_w$  while  $c_{ds}$  controls the TKE injection associated with wave energy dissipation through whitecapping.

		Mixing	g length
		$\alpha_w = 1$	$\alpha_w = 0.5$
F	$c_{ds} = 1$	Rref	Rturb2
$F_K$	$c_{ds} = 0$	Rturb1	Rturb3

530

Under storm conditions, whitecapping explains more than two-third of the TKE injected at the surface in regions I and II. This greatly affects the mixing in the upper third of 531 the water column (see  $\nu$  almost doubled at some locations between Rref and Rturb1 in Fig. 532 7). Note, however, that it only slightly impacts the cross-shore circulation (RD( $\hat{u}) \leq 7\%$ , see 533

the comparisons Rturb1/Rref and Rturb3/Rturb2 in Table 2), with the largest differences 534 being found in the upper part of the water column. Furthermore, in both high or moderate 535 wave energy conditions, the model shows a strong sensitivity to the parameterization of the 536 surface mixing length, which strengthens as the injection of TKE at the surface increases 537 closer to shore (within the zones II and III, see Table 2). With a shorter surface mixing 538 length, the eddy viscosity at the surface is weaker, such that the cross-shore velocity profiles 530 are more sheared (see Fig. 7 under high wave energy conditions, while similar results -540 not shown - are found under moderate wave energy conditions). As a result, the orienta-541 tion of the cross-shore flow near the surface even changes for one profile within the zone II 542 under high energy condition with a shorter mixing length. The relative difference on the 543 cross-shore velocity reaches 32% depending on the parameterization of  $z_0^s$ . Interestingly, 544 comparing Rturb2/Rref and Rturb3/Rturb1 tends to show that the sensitivity to the pa-545 rameterization of the surface mixing length is stronger depending on the contribution of the 546 whitecapping to the TKE injection (see Table 2). Overall, it appears that the parameteri-547 zation of the TKE injection impacts the vertical shear of the cross-shore velocity as far as 548 6 km from the shoreline under energetic conditions. 549



Figure 7. Vertical profiles of turbulent kinetic energy (K, panel **a**), vertical eddy viscosity ( $\nu$ , panel **b**) and quasi-Eulerian cross-shore velocity ( $\hat{u}$ , panel **c**). The results are presented for the four configurations of the model (see Table 1) and are extracted under high wave energy conditions. The delimited zones are defined in section 5.1

**Table 2.** Relative difference (in %)  $\operatorname{RD}_{1/2}(X) = \overline{|\hat{X}_1 - \hat{X}_2|}/|\overline{\hat{X}_2|}$  of modelled turbulent kinetic energy (K), vertical eddy viscosity ( $\nu$ ) and cross-shore velocity ( $\hat{u}$ ) vertical profiles for the different configurations of the model within the three delimited area introduced in section 5.1, under high (HE) or moderate (LE) wave energy conditions. High RD values indicate a strong sensitivity to turbulence settings, either to the mixing length or the surface flux of TKE.

		Rturb1/Rref	Rturb3/Rturb2	Rturb2/Rref	Rturb3/Rturb1
	zone I				
HE	RD(K)	92	88	30	5
	$\mathrm{RD}(\nu)$	62	49	42	8
	$\mathrm{RD}(\hat{u})$	3	6	12	4
	zone II				
	RD(K)	60	56	27	21
	$\mathrm{RD}(\nu)$	25	23	41	28
	$\mathrm{RD}(\hat{u}$	7	4	28	19
	zone III				
	RD(K)	2	2	16	16
	$\mathrm{RD}(\nu)$	<1	<1	29	29
	$\mathrm{RD}(\hat{u})$	<1	<1	30	30
	zone I				
	RD(K)	66	60	25	12
LE	$\mathrm{RD}(\nu)$	26	18	26	12
	$\mathrm{RD}(\hat{u})$	2	2	10	7
	zone II				
	RD(K)	30	28	24	21
	$\mathrm{RD}(\nu)$	10	9	29	25
	$\mathrm{RD}(\hat{u})$	2	2	32	27
	zone III				
	RD(K)	4	3	16	16
	$\mathrm{RD}(\nu)$	<1	<1	29	29
	$\mathrm{RD}(\hat{u})$	<1	<1	30	29

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#### 5.3 Wave-induced circulation patterns and forcing mechanisms

Under moderate wave energy conditions, non-conservative breaking wave forces arise 551 relatively close to shore, up to 1 km from the shoreline (Fig. 8a) and are mostly associated 552 with depth-induced breaking, which dominates the wave energy dissipation within the zones 553 II and III (Fig. 6b). The quasi-Eulerian cross-shore flow therefore shows a strong seaward-554 directed current reaching  $0.3 \,\mathrm{m/s}$  in the lower part of the water column, whereas a shoreward-555 directed current arises near the surface (Fig. 8c). The depth-averaged quasi-Eulerian cross-556 shore flow (i.e. the undertow) nearly compensates for the depth-averaged cross-shore Stokes 557 drift velocity component (the divergence of the alongshore velocity component is not exactly 558 zero), while the depth-varying cross-shore flow is locally strengthened by the effect of the 559 non-conservative breaking wave forces within the zones II and III, resulting in a 100%560 stronger seaward-directed current in the lower part of the water column than the surface 561 Stokes drift velocity (Fig. 8b-c and 10b). In order to better evaluate the contribution of 562 breaking, an additional run was performed with the non-conservative breaking wave forces 563 uniformly distributed over the vertical (RF<sub>br</sub>). The resulting quasi-Eulerian cross-shore 564 flow is less sheared near the surface within the zones II and III, yielding a weaker seaward-565 directed current in the lower part of the water column than that obtained with a near surface 566 momentum source by up to a factor three (Fig. 10b). Within zone I, the quasi-Eulerian 567 cross-shore flow is also mostly seaward-directed, with a maximum intensity in the upper 568 part of the water column, while a weak shoreward-directed current associated with wave 569 streaming arises near the bottom and extends inside the zone II (Fig. 8a,c and 10b). As a 570 result, a strong clockwise Lagrangian overturning circulation develops within the zones II 571 and III (the magnitude of the current locally reaches  $0.3 \,\mathrm{m/s}$ ), while a weaker anti-clockwise 572 overturning cell arises at the seaward edge of the zone II, which constrains the offshore flow 573 (see the upward deflection of the streamlines of the clockwise cell within the zone II in Fig. 574 8d). A similar circulation patern in the vicinity of the surf zone was found by Wang et 575 al. (2020). The magnitude of the Lagrangian circulation then decreases relatively rapidly 576 within zone I (Fig. 8d). Interestingly, the cross-shore quasi-Eulerian flow does not exactly 577 compensate for the cross-shore Stokes drift velocity component, which would have been 578 expected assuming a balance between the Coriolis force associated with the quasi-Eulerian 579 flow and the Stokes-Coriolis force, as pointed out by Lentz et al. (2008). Presumably, this 580 could be attributed to the shape of the coastline, which is not alongshore-uniform at the 581 scale of several kilometers, the distance where the instruments were located. 582

583	Under high wave energy conditions, non-conservative breaking wave forces arise at the
584	surface as far as $6\mathrm{km}$ from the shoreline and strengthen shoreward (Fig. 9a), associated with
585	a significant wave energy dissipation occurring through white capping and depth-induced
586	breaking within the zones II and III (Fig. 6a). The quasi-Eulerian cross-shore flow shows a
587	strong seaward-directed current of the order of $0.2\mathrm{m/s}$ up to $4\mathrm{km}$ from the shoreline, whose
588	intensity progressively decreases offshore reaching $0.1\mathrm{m/s}$ as far as $10\mathrm{km}$ from the shoreline
589	(Fig. 9c). Similar to moderate wave energy conditions, this current is strengthened locally
590	by the effect of the non-conservative breaking wave forces within the zones II and III (Fig. $$
591	10a). Interestingly, no near-bottom shoreward-directed current arises as the intensity of the $% \left( {{{\left[ {{{\left[ {{\left[ {{\left[ {{\left[ {{{\left[ {{{c}}} \right]}}} \right]}$
592	bottom streaming decreases beyond 20 m-depth, while closer to shore the cross-shore flow
593	in the lower part of the water column is dominated by the strong seaward-directed current.
594	The Lagrangian circulation therefore shows a wide clockwise overturning cell extending over
595	$8\mathrm{km},$ which generates a seaward-oriented jet in the lower part of the water column (Fig. 9d)
596	that contrasts with the circulation patern obtained under moderate wave energy conditions.



Figure 8. Cross-shore profiles under moderate wave energy conditions of the wave force crossshore component, which includes the Stokes-Coriolis term, the vortex force, the wave-induced pressure term and the non-conservate wave forces (a), the Stokes drift velocity cross-shore component (b), the quasi-Eulerian velocity cross-shore component (c), and the 2DV Lagrangian circulation streamlines and magnitude (d). For readability, S-level indices are used for representing the wave force profile (the level 0 corresponds to the bottom and the level 24 to the free surface). Note that the cross-shore distance axis here extends over 2 km.



Figure 9. Same as Figure 8 under high wave energy conditions. Note that the cross-shore distance axis here extends over 12 km.



Figure 10. Vertical profiles of the Stokes drift velocity cross-shore component  $(u_S)$  and the quasi-Eulerian cross-shore velocity  $(\hat{u})$  under high (a) or moderate (b) wave energy conditions for the baseline run (Rref) and for a run performed with the non-conservative breaking wave forces uniformly distributed (RF<sub>br</sub>). The delimited zones are defined in section 5.1.

#### <sup>597</sup> 6 Conclusions and perspectives

In this study, we presented a dataset comprising water levels, wave parameters and 598 currents collected under fair weather and storm conditions issued from a field campaign 599 carried out in early 2021 within the shoreface and the surf zone of the dissipative beach of 600 Saint-Trojan (France). These results were complemented with the predictions from a state-601 of-the-art wave-averaged 3D circulation modelling system coupling the circulation model 602 SCHISM (Y. J. Zhang et al., 2016) with the spectral wave model WWM (Roland et al., 603 2012) in order to study the wave-induced cross-shore circulation in the nearshore area up 604 to the surf zone. Both measurements and model results clearly showed that the cross-605 shore flow is dominated by a strong seaward-directed current in the lower part of the water 606 column, which under storm wave conditions can reach  $0.2 \,\mathrm{m/s}$  as far as  $4 \,\mathrm{km}$  from the 607 shoreline. The model was further employed to study the driving mechanisms of the wave-608

induced cross-shore circulation. It was shown that a wide ( $\simeq 6 \,\mathrm{km}$ ) transition zone appears 609 under high wave energy conditions where depth-induced breaking, whitecapping and bottom 610 friction all contribute significantly to the wave energy dissipation, whereas the surf zone 611 edge appears clearly delimited under moderate wave energy conditions. Once wave energy 612 dissipation through breaking processes starts being substantial, sensitivity tests performed 613 with the model tended to show that the parameterization of the wave-enhanced mixing could 614 substantially impact the vertical shear of the cross-shore velocity close to the surface, while 615 non-conservative breaking wave forces strengthen locally the seaward-directed current in the 616 lower part of the water column. The wave-induced cross-shore circulation thus presents very 617 contrasting patterns. Under moderate wave energy conditions, the dominance of the wave 618 energy dissipation by bottom friction seaward of the surf zone allows the development of a 619 near-bottom onshore flow associated with bottom streaming of the order of a few centimetres 620 per second. Thus, the surf zone clockwise Lagrangian overturning circulation weakens, while 621 an additional anti-clockwise overturning cell arises seaward of the surf zone and extends 622 within it. In contrast, under high energy conditions the Lagrangian circulation shows a 623 seaward-directed jet in the lower part of the water column, whose intensity progressively 624 decreases offshore. Among different implications, this study opens perspectives for sediment 625 transport modelling using a similar 3D framework in order to produce realistic morphological 626 evolutions across the shoreface. 627

#### 628

#### Code and Data Availability Statement

The processed field data presented in this paper are available through a Zenodo repository (Pezerat et al., 2022). The instructions to download and install the model used in this study can be accessed freely at https://github.com/schism-dev/schism. Figures were made with python module Matplotlib version 3.1.1, available under the Matplotlib licenses at https://matplotlib.org/.

#### Appendix A Vortex force framework in the modelling system SCHISM

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In the vortex force framework the continuity and momentum equations read:

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$$\frac{\partial \hat{u}}{\partial x} + \frac{\partial \hat{v}}{\partial y} + \frac{\partial \hat{w}}{\partial z} = 0 \tag{A1}$$

$$\frac{D\hat{u}}{Dt} - f\hat{v} = -\frac{1}{\rho}\frac{\partial P_H}{\partial x} + \frac{\partial}{\partial z}\left(\nu\frac{\partial\hat{u}}{\partial z}\right) + v_S\left(f_C + \left(\frac{\partial\hat{v}}{\partial x} - \frac{\partial\hat{u}}{\partial y}\right)\right) - w_S\frac{\partial\hat{u}}{\partial z} - \frac{\partial J}{\partial x} + \hat{F}_x$$
(A2)

$$\frac{D\hat{v}}{Dt} + f\hat{u} = -\frac{1}{\rho}\frac{\partial P_H}{\partial y} + \frac{\partial}{\partial z}\left(\nu\frac{\partial\hat{v}}{\partial z}\right) - u_S\left(f_C + \left(\frac{\partial\hat{v}}{\partial x} - \frac{\partial\hat{u}}{\partial y}\right)\right) - w_S\frac{\partial\hat{v}}{\partial z} - \frac{\partial J}{\partial y} + \hat{F}_y \quad (A3)$$

where  $[\hat{u}, \hat{v}, \hat{w}]$  is the quasi-Eulerian velocity, equal to the mean Lagrangian velocity [u, v, w]minus the Stokes drift velocity  $[u_S, v_S, w_S]$ . In Eqs A2 and A3,  $f_C$  is the Coriolis parameter,  $\rho$  is the water density, g is the gravitational acceleration,  $\nu$  is the vertical eddy viscosity,  $P_H$  is the hydrostatic pressure, J is the wave-induced mean pressure and  $[\hat{F}_x, \hat{F}_y]$  gathers the non-conservative wave forces.

The three components of the Stokes drift velocities, the wave-induced pressure term and the non-conservative wave forces are all computed from local variables issued from WWM, which simulates the generation, propagation and transformation of short waves by solving the Wave Action Equation (e.g. Komen et al., 1994):

$$\frac{\partial N}{\partial t} + \frac{\partial}{\partial x} \left( (C_{g,x} + \tilde{u})N) + \frac{\partial}{\partial y} \left( (C_{g,y} + \tilde{v})N) + \frac{\partial(\dot{\sigma}N)}{\partial \sigma} + \frac{\partial(\dot{\theta}N)}{\partial \theta} = S_{tot} \right)$$
(A4)

where  $\sigma$  is the relative wave frequency, which is related to the wavenumber k by the linear 651 dispersion relation;  $\theta$  corresponds to the wave direction;  $N = \rho g E / \sigma$  is the wave action 652 density spectrum, with E the sea surface elevation density spectrum;  $[C_{g,x}, C_{g,y}]$  is the 653 intrisic group velocity;  $[\tilde{u}, \tilde{v}]$  is the advective current velocity, here equal to the depth-654 averaged horizontal quasi-Eulerian velocity. Finally,  $S_{tot}$  is a sum of source terms that 655 account for the energy input due to wind, non linear wave-wave interactions, and energy 656 dissipation due to whitecapping, depth-induced breaking and bottom friction (cf. section 657 3.1).658

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The horizontal Stokes drift velocity vector is given by:

$$[u_S, v_S] = \int_{\sigma} \int_{\theta} \sigma' k E \frac{\cosh(2k(z+d))}{\sinh^2(kh)} [\cos\theta', \sin\theta'] d\sigma' d\theta'$$
(A5)

where  $h = d + \bar{\eta}$  is the (local) phase-averaged water depth (with d, the still water depth and  $\bar{\eta}$ , the phase-averaged free surface elevation). The vertical Stokes drift component is given by the horizontal divergence of  $[u_S, v_S]$  as the full Stokes drift flow is non divergent at the lowest order (Ardhuin et al., 2008). The wave-induced pressure term reads:

$$J = \int_{\sigma} \int_{\theta} \frac{gkE}{\sinh(2kh)} d\sigma' d\theta'$$
(A6)

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Finally, the formulation of the non-conservative wave forces are detailed in section 3.2.1.

The wave model is supplemented by a roller model that helps representing the inertia of depth-induced breaking processes by slightly advecting the location where energy is actually dissipated towards the shoreline (Svendsen, 1984b). As compared to the implementation detailled in Guérin et al. (2018), the roller model solves a balance equation for the roller kinetic energy  $E_R$  (e.g Reniers et al., 2004), slightly modified to account for the modification of the wave phase velocity by the mean current within the advection term, such that:

$$\frac{\partial E_R}{\partial t} + \frac{\partial}{\partial x} \left( 2E_R(c_x + \tilde{u}) \right) + \frac{\partial}{\partial y} \left( 2E_R(c_y + \tilde{v}) \right) = \alpha_R D_{db} - D_R \tag{A7}$$

where  $[c_x, c_y]$  is the wave phase velocity computed by means of the short wave (continuous) peak wavenumber  $(k_p)$  and mean direction  $(\theta_m)$ ;  $D_{db}$  is the bulk wave energy dissipation rate by depth-induced breaking;  $\alpha_R$  is the percentage of wave energy dissipation by depthinduced breaking transferred to the rollers (Tajima & Madsen, 2006) and  $D_R$  is the roller energy dissipation rate, which reads:

$$D_R = \frac{2g\sin\beta_R E_R}{\sqrt{c_x^2 + c_y^2}} \tag{A8}$$

where  $\sin \beta_R = 0.1$  is the roller angle (Nairn et al., 1991; Reniers et al., 2004). Surface rollers contribute to the total mass flux in proportion to the roller energy. Although this transport primarily occurs near the surface, above trough level, there is no consensus on its vertical distribution. We here follow the choice to impose an homogeneous vertical distribution. This contribution is accounted for through an additional term in the horizontal Stokes drift velocity vector, which reads:

$$[u_{S,R}, v_{S,R}] = \frac{2E_R}{\rho h \sqrt{c_x^2 + c_y^2}} [\cos \theta_m, \sin \theta_m] \ \forall \ z \in [-d, \bar{\eta}]$$
(A9)

Note, however, that  $w_S$  is still computed with  $u_S$ ,  $v_S$  from Eq. A5 as it is assumed that rollers do not contribute to the vertical transport.

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